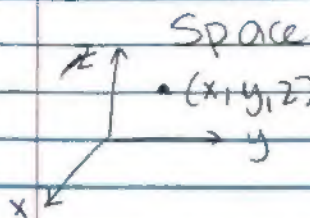


## 12.1 coordinate systems in 3D



Space

$(x, y, z)$

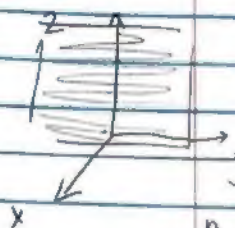
3-Space =  $\mathbb{R}^3$

Notation:  $\{(x, y, z) \in \mathbb{R}^3\}$

### I - coordinate planes

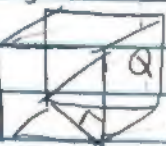
- a coordinate plane in  $\mathbb{R}^3$  is a set of planes all which have a coordinate of zero

ie:  $(x, y, 0)$ ,  $(x, 0, z)$ ,  $(0, y, z)$



### A - Distances in 3-Space

Distance formula:



$P = (x_0, y_0, z_0)$

$Q = (x, y, z)$

$$\sqrt{(x-x_0)^2 + (y-y_0)^2 + (z-z_0)^2}$$

### II - Spheres

Let  $P = (x_0, y_0, z_0)$  in  $\mathbb{R}^3$  and  $r > 0$ .

The sphere centered at  $P$

and radius  $r$  is  $S = \{(x, y, z) \in \mathbb{R}^3 :$

$$\sqrt{(x_0-x)^2 + (y_0-y)^2 + (z_0-z)^2} = r \}$$

## 12.2 vectors

Vector in  $\mathbb{R}^3$  is a directed line segment

example shown in  $\mathbb{R}^2$

$(0, 0)$  tail

head  $(1, 1)$

vectors are equiv. when they are linear shifts of each other

ex:  $(0, 0) \rightarrow (1, 0) = (2, 0) \rightarrow (3, 0)$